## UIC Math 180, Fall 2012

1. Find the following limits.

(a)  $\lim_{x \to 1} 3e^x$ 

(b) 
$$\lim_{x \to -3} \frac{x^2 + 4x + 3}{x + 3}$$

(c) 
$$\lim_{x \to 0} \frac{1 - \sqrt{1 + x^2}}{x^2}$$

(d) 
$$\lim_{x \to 1} \frac{1 - \sqrt{3 - x}}{x + 2}$$

(e) 
$$\lim_{x \to -\infty} \frac{\sqrt{x^2 + 3}}{7 - 2x}$$

(f) 
$$\lim_{x \to 1^{-}} \frac{1}{(x-1)^2}$$

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- 2. Complete the formal definition of continuity. The function f(x) is *continuous at* x = a if
- 3. On which intervals are the following functions continuous?

(a) 
$$\frac{1}{x-1} + 1$$

(b) 
$$\sqrt{1-x^2}-2$$

(c) 
$$\frac{(x-1)(x-2)}{(x-3)(x-4)}$$

(d) 
$$\frac{\sin(x)}{\cos(x)}$$

4. For which value(s) of k is the function 
$$f(x) = \begin{cases} 4 - kx & \text{if } x > 1, \\ x^2 + k & \text{if } x \le 1 \end{cases}$$
 continuous?

5. (a) Write the formal definition of the derivative.

f'(a) =

(b) Use the formal definition of the derivative to prove that  $\frac{d}{dx}\sqrt{x} = \frac{1}{2\sqrt{x}}$ .

6. (a) Write the quotient rule for derivatives:

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) =$$

(b) Use to quotient rule to prove that  $\frac{d}{dx}\cot(x) = -\csc^2(x)$ .

7. Find the following derivatives.

(a) 
$$\frac{d}{dx}\sqrt{\cos(x)}$$

(b) 
$$\frac{d}{dt}\frac{1}{1+e^{-t}}$$

(c) 
$$\frac{d}{dx} \frac{x^2 - 3e^x}{(x-2)^2}$$

(d) 
$$\frac{d}{dx}\frac{4x-3}{\sqrt{x^2-1}}$$

(e) 
$$\frac{d}{dx} \left( e^{\sin(x)} - x\cos(x) \right)$$

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8. Find the equation of the tangent line at  $x = -\pi$  to the graph of

$$f(x) = \frac{\sin(x) + 1}{x}$$

9. Find  $\lim_{x\to 0} x^2 \sin\left(\frac{1}{x}\right)$  and prove that your answer is correct using the squeeze theorem.